

Section
5.2D

Choose values for a and b and use decimal approximations in your calculator to explore whether the following statements are **true** or **false**. Repeat with at least one other set of values for a and b . Justify your answer. Caution: finding some values for which the statement is true does not make the statement true. However, finding a single example where the statement is not true proves the entire statement false.

When completed, compare your results with other groups in class. Make a conjecture for each statement, based on this data.

| Equation Conjecture | First set of values: $a = 5$ $b = 4$ | Second set of values: $a = 12$ $b = 16$ | Equation Conjecture |
|---|---|---|--|
| 1) $\sqrt{a \cdot b} = \sqrt{a} \cdot \sqrt{b}$ | $\sqrt{5 \cdot 4} = \sqrt{5} \sqrt{4}$ True False (circle one) | $\sqrt{12 \cdot 16} = \sqrt{12} \sqrt{16}$ True False (circle one) | $\sqrt{a \cdot b} = \sqrt{a} \cdot \sqrt{b}$ True False |
| 2) $\sqrt{a + b} = \sqrt{a} + \sqrt{b}$ | $\sqrt{5 + 4} = \sqrt{5} + \sqrt{4}$ True False (circle one) | $\sqrt{12 + 16} = \sqrt{12} + \sqrt{16}$ True False (circle one) | $\sqrt{a + b} = \sqrt{a} + \sqrt{b}$ True False |

Section
5.2D

Choose values for a and b and use decimal approximations in your calculator to explore whether the following statements are **true** or **false**. Repeat with at least one other set of values for a and b . Justify your answer. Caution: finding some values for which the statement is true does not make the statement true. However, finding a single example where the statement is not true proves the entire statement false.

When completed, compare your results with other groups in class. Make a conjecture for each statement, based on this data.

| Equation Conjecture | First set of values: $a = 5$ $b = 4$ | Second set of values: $a = 3$ $b = 9$ | Equation Conjecture |
|---|---|---|--|
| 3) $\sqrt{a - b} = \sqrt{a} - \sqrt{b}$ | True False (circle one) | True False (circle one) | $\sqrt{a - b} = \sqrt{a} - \sqrt{b}$ True False |
| 4) $\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$ | $\sqrt{\frac{5}{4}} = \frac{\sqrt{5}}{\sqrt{4}}$ True False (circle one) | $\sqrt{\frac{3}{9}} = \frac{\sqrt{3}}{\sqrt{9}}$ True False (circle one) | $\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$ True False |

#1 – 6: Simplify the following. Show your work.

$$\begin{aligned} 1) \sqrt{20} &= \sqrt{4 \cdot 5} \\ &= \sqrt{4} \cdot \sqrt{5} \\ &= \boxed{2\sqrt{5}} \end{aligned}$$

$$\begin{aligned} 2) \sqrt{50} &= \sqrt{25 \cdot 2} \\ &= \sqrt{25} \cdot \sqrt{2} \\ &= 5\sqrt{2} \end{aligned}$$

$$\begin{aligned} 3) \sqrt{18} &= \sqrt{9 \cdot 2} \\ &= 3\sqrt{2} \end{aligned}$$

1
4
9
16
25
36
49
64
81
100

$$\begin{aligned} 4) \sqrt{75} &= \sqrt{25 \cdot 3} \\ &= 5\sqrt{3} \end{aligned}$$

$$\begin{aligned} 5) \sqrt{48} &= \sqrt{16 \cdot 3} \\ &= 4\sqrt{3} \end{aligned}$$

$$\begin{aligned} 6) \sqrt{700} &= \sqrt{100 \cdot 7} \\ &= 10\sqrt{7} \end{aligned}$$

Products and quotients involving radicals: Things inside and outside of radicals cannot simply be multiplied or divided.

| | |
|---|---|
| <p><i>Example 5:</i></p> <p>Simplify $3\sqrt{12}$</p> <p><i>Answer:</i></p> $3\sqrt{12} = 3\sqrt{4 \cdot 3} = 3 \cdot 2\sqrt{3} = 6\sqrt{3}$ | <p><i>Example 6:</i></p> <p>Simplify $\frac{\sqrt{32}}{2}$</p> <p><i>Answer:</i></p> $\frac{\sqrt{32}}{2} = \frac{\sqrt{16 \cdot 2}}{2} = \frac{4\sqrt{2}}{2} = 2\sqrt{2}$ |
|---|---|

#16 – 18: Simplify (some of these may already be simplified)

$$\begin{aligned} 16) 4\sqrt{20} &= 4 \cdot \sqrt{20} \\ &= 4 \cdot 2\sqrt{5} \\ &= \boxed{8\sqrt{5}} \end{aligned}$$

$$17) \frac{\sqrt{72}}{9}$$

$$18) \frac{4 + \sqrt{28}}{2}$$

Simplify the expression:

page 18

1. $4\sqrt{20}$

$$(8\sqrt{5})$$

$$\begin{aligned} &= \frac{\sqrt{9 \cdot 5}}{6} \\ &= \frac{\sqrt{9} \cdot \sqrt{5}}{6} \\ &= \frac{3 \cdot \sqrt{5}}{6} \\ &= \frac{1\sqrt{5}}{2} \end{aligned}$$

2. $\frac{\sqrt{45}}{6}$

3. $\frac{6+2\sqrt{8}}{2}$

$$\begin{aligned} &\frac{6 + 2 \cdot 2\sqrt{2}}{2} \\ &= \frac{6 + 4\sqrt{2}}{2} \\ &= \frac{6}{2} + \frac{4\sqrt{2}}{2} \\ &= 3 + 2\sqrt{2} \end{aligned}$$

Note: $\sqrt{8} = \sqrt{4 \cdot 2} = \sqrt{4} \cdot \sqrt{2} = 2 \cdot \sqrt{2}$

Simplify the expression:

4. $\frac{5+8\sqrt{20}}{10}$

5. $\frac{14+\sqrt{36}}{2}$

6. $\frac{14+7\sqrt{100}}{2}$

$$\begin{aligned} &\frac{14+6}{2} \\ &= \frac{20}{2} \\ &= 10 \end{aligned}$$